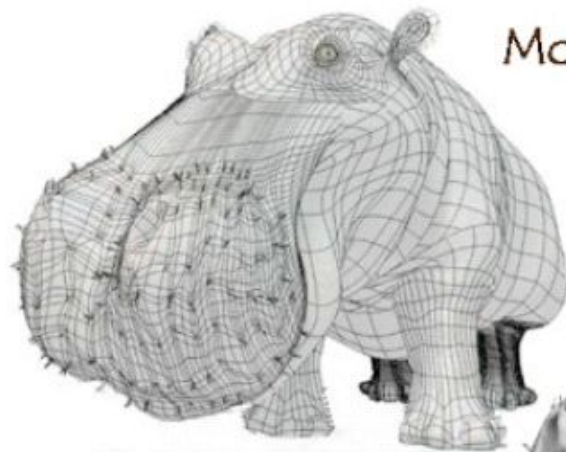


3: textures

1. Quest for Visual Realism



Model



Model + Shading



Model + Shading
+ Textures



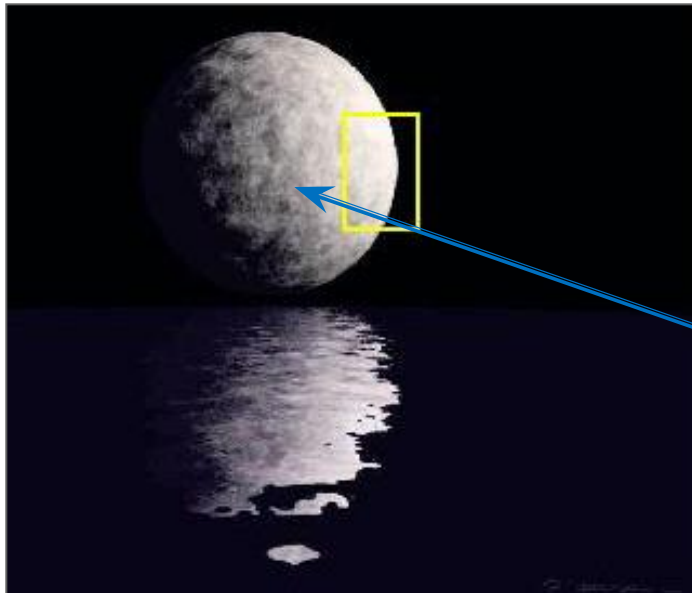
At what point
do things start
looking real?

Need for fine details in color variation!

Motivations

2. Limit the number of polygons

Problem: Everything cannot be modeled at the scale of geometry!



Micro-polygons
would be needed!

Textures

Modeling changes of material

Enable the material attributes to vary inside a face

- The local attribute will be used during rendering

Examples of attributes: color, shininess, normals, transparency...

Still a single face,
but several colors



Textures

Modeling changes of material

Enable the material attributes to vary inside a face

- The local attribute will be used during rendering

Examples of attributes: color, shininess, normals, transparency...

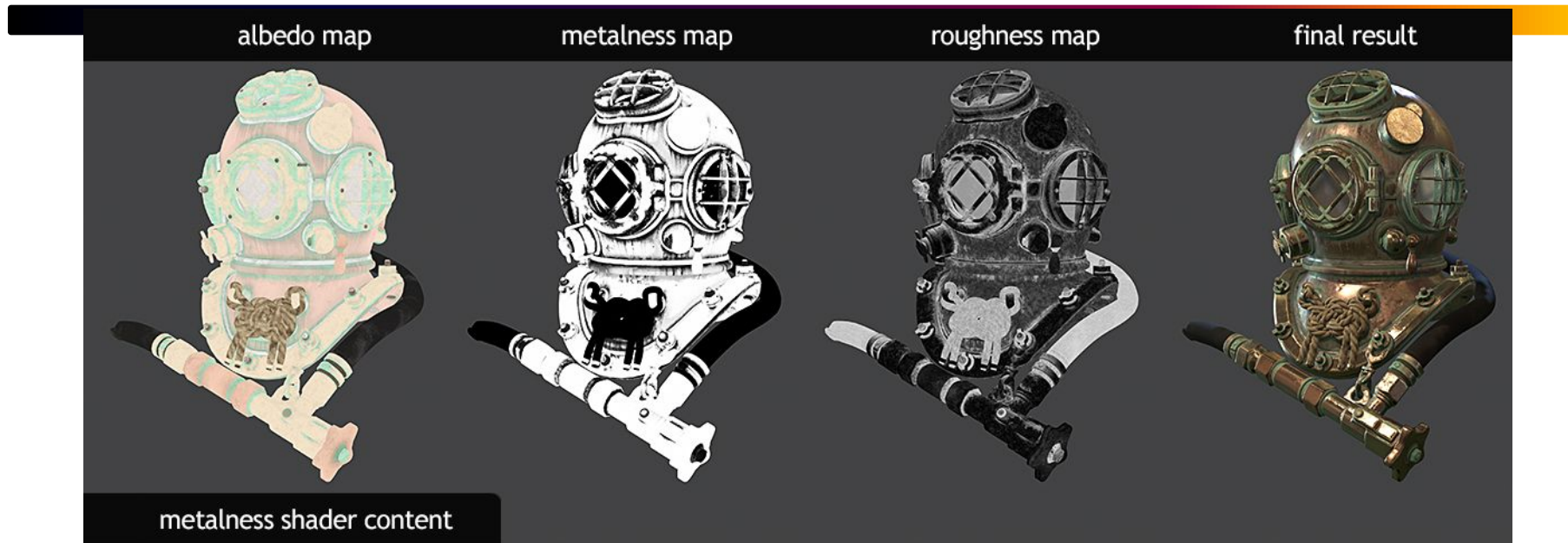
Typically:

$$L(\mathbf{p} \rightarrow \mathbf{e}) = K_a + \sum_s [K_d(\mathbf{n} \cdot \boldsymbol{\ell}) + K_s(\mathbf{r} \cdot \mathbf{e})^n] I_s$$

ambient diffuse specular

Textures

Modeling changes of material



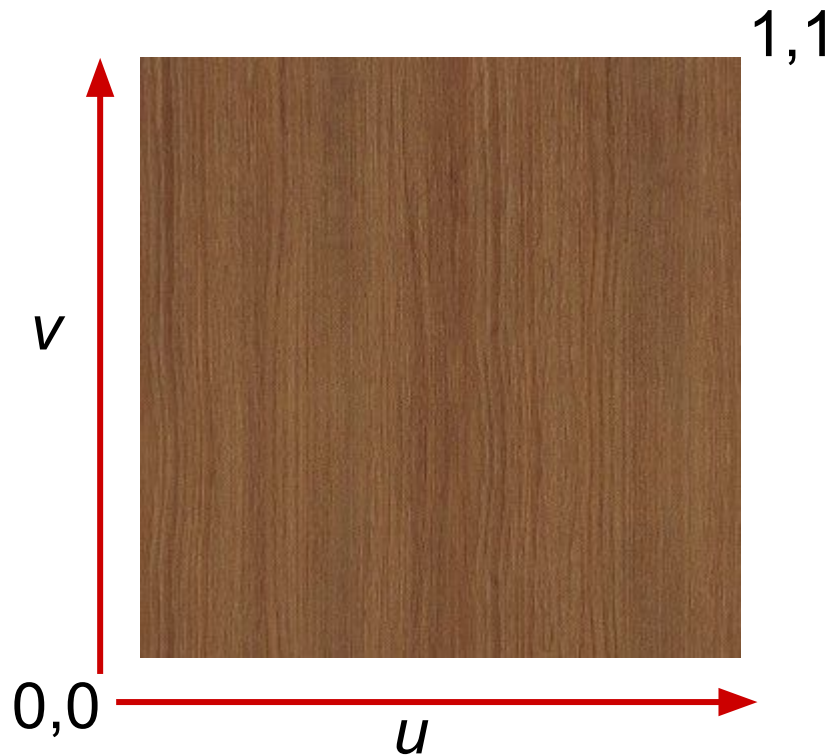
<https://www.marmoset.co/posts/pbr-texture-conversion/>

$$L(\mathbf{p} \rightarrow \mathbf{e}) = K_a + \sum_s [K_d(\mathbf{n} \cdot \mathbf{l}) + K_s(\mathbf{r} \cdot \mathbf{e})^n] I_s$$

ambient diffuse specular

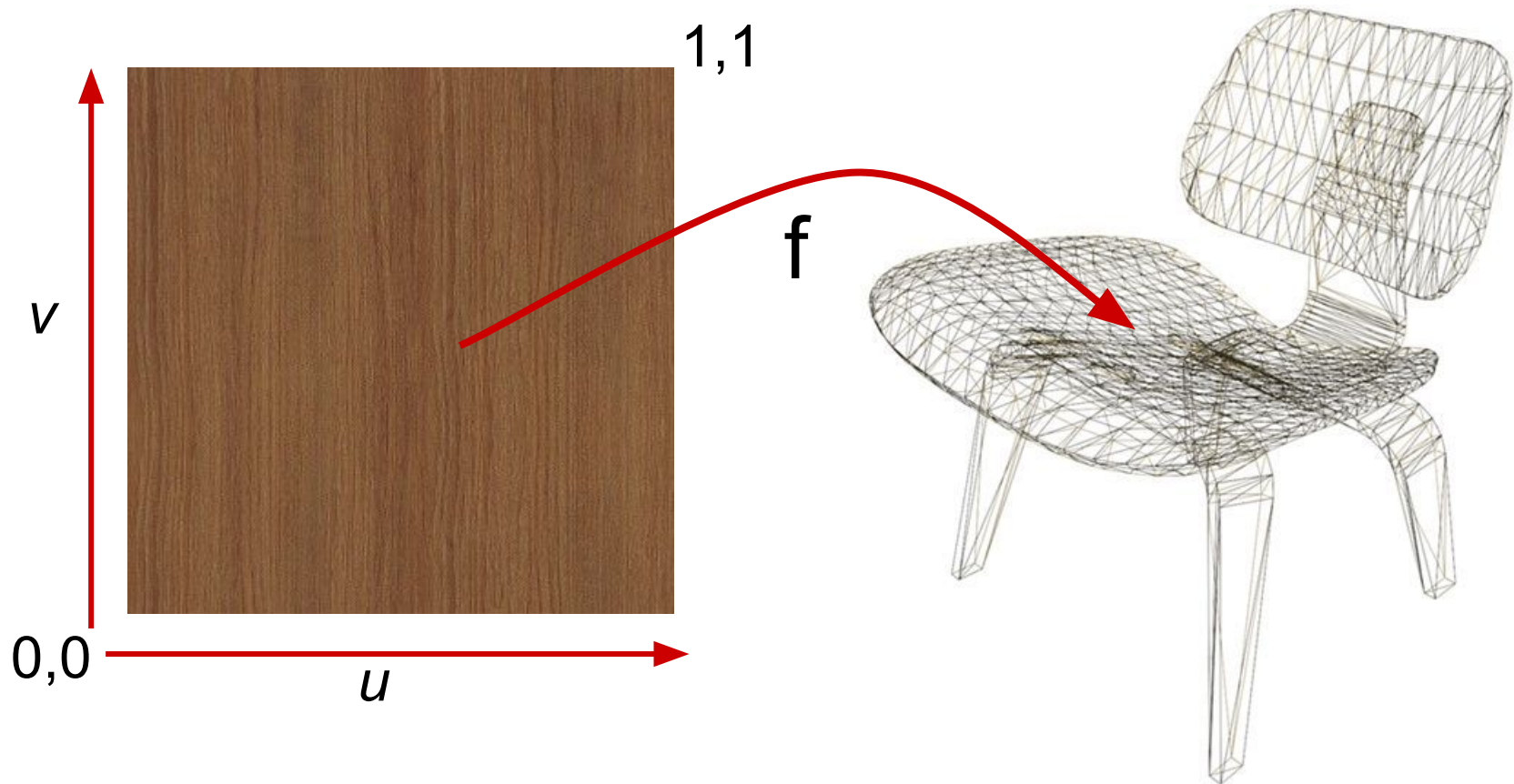
2D Textures: picture of attributes + mapping

- Planar image $I(u,v)$



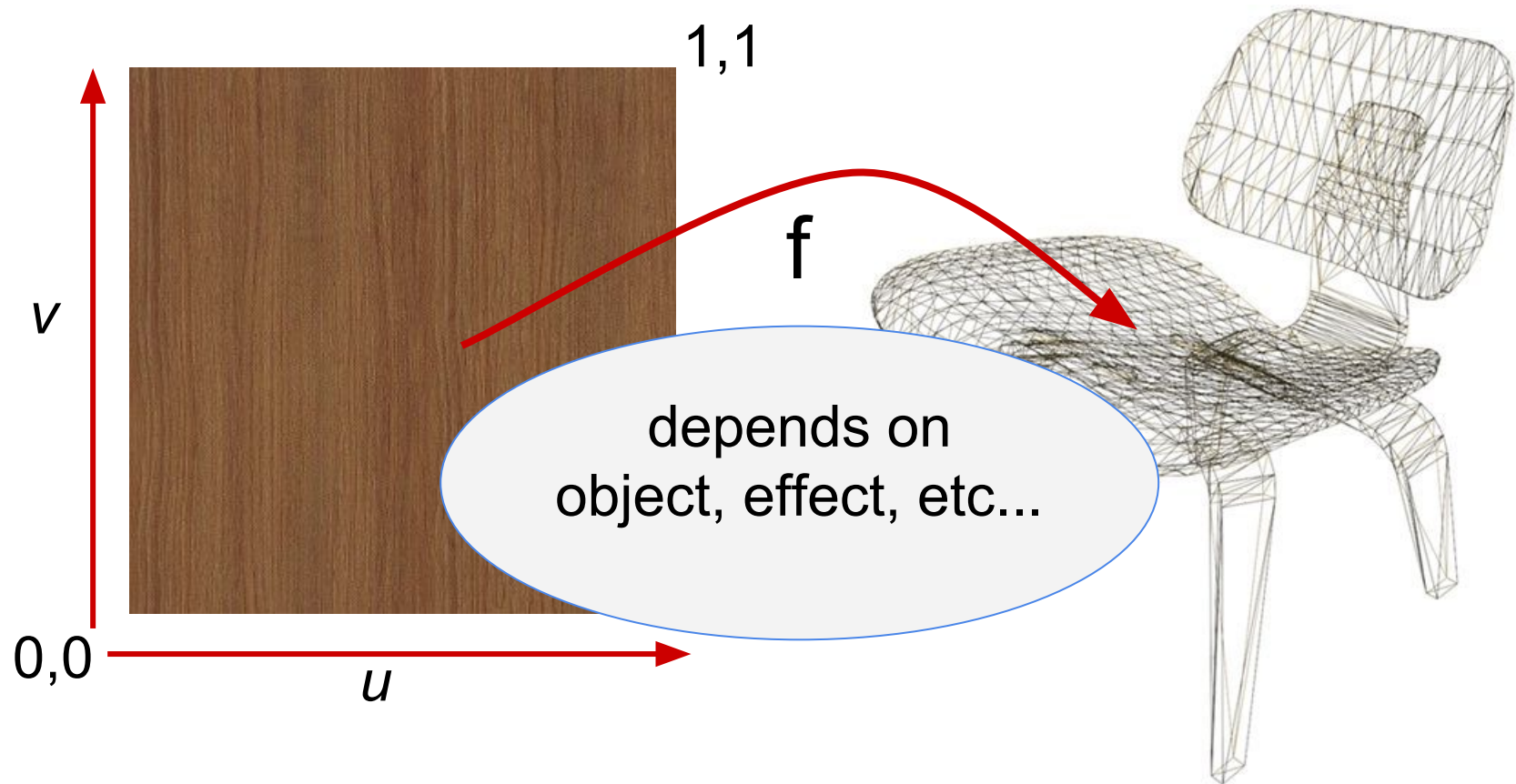
2D Textures: picture of attributes + mapping

- Planar image $I(u,v)$ + mapping $f: P(x,y,z) \rightarrow (u,v)$



2D Textures: picture of attributes + mapping

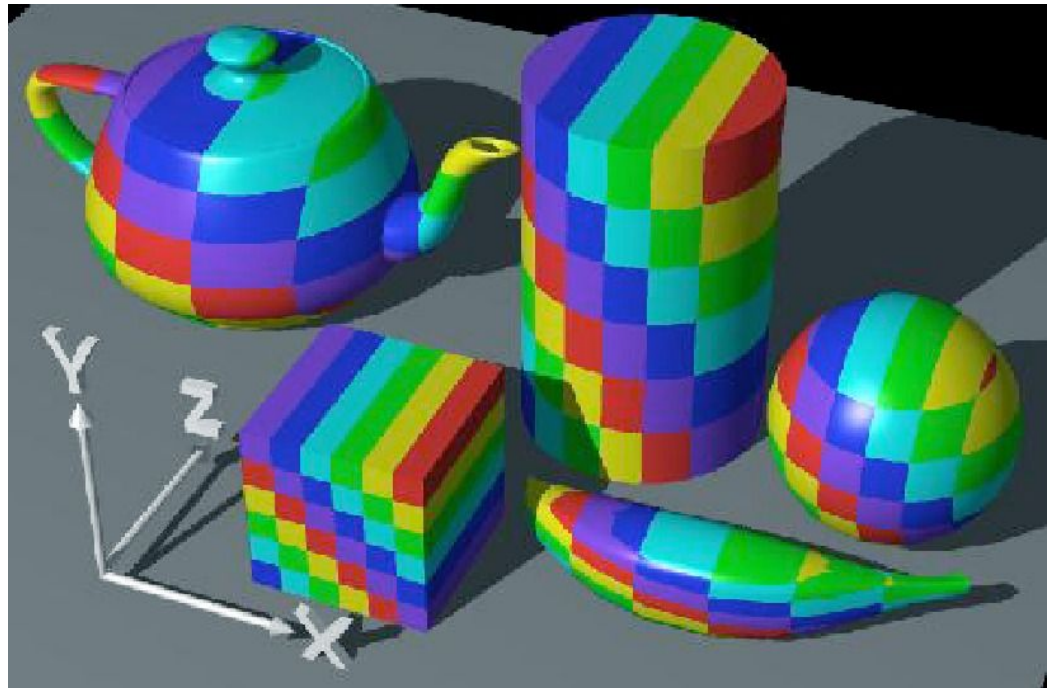
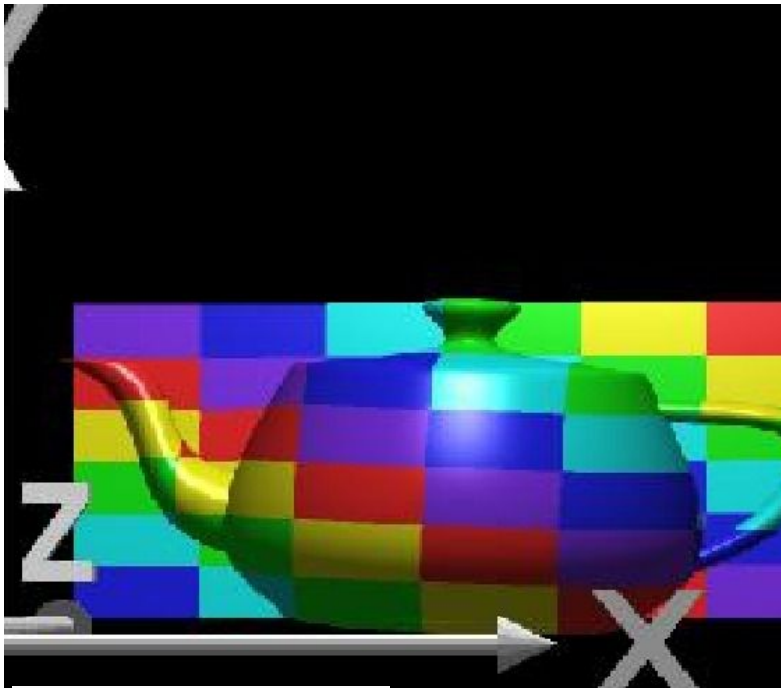
- Planar image $I(u,v)$ + mapping $f: P(x,y,z) \rightarrow (u,v)$



Mapping function: flat/planar mapping

$$f: (x,y,z) \rightarrow [0,1] \times [0,1]$$

- Planar mapping: $\mathbf{f}(x,y,z) = (x, y)$



Mapping function: projective mapping

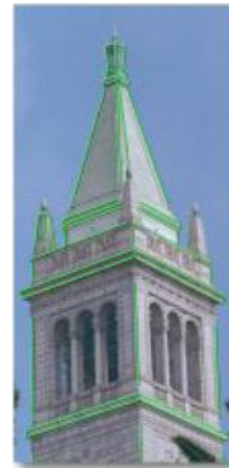
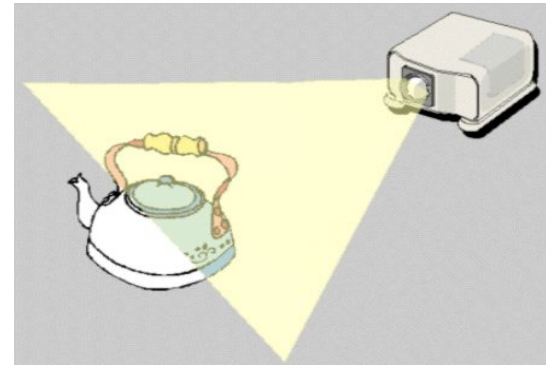
Map the texture like with a slide projector

Advantage

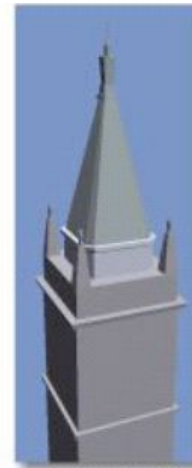
- No need for texture coordinates!

Inc

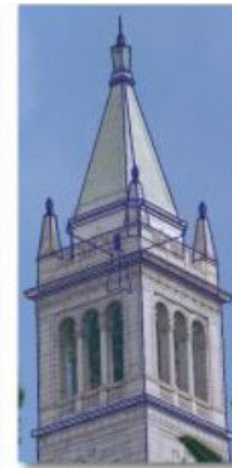
- One viewpoint
- Distortions
- Blending



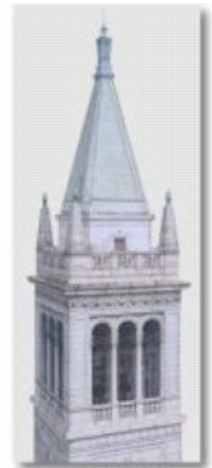
Original photograph with marked edges



Recovered model



Model edges projected onto photograph

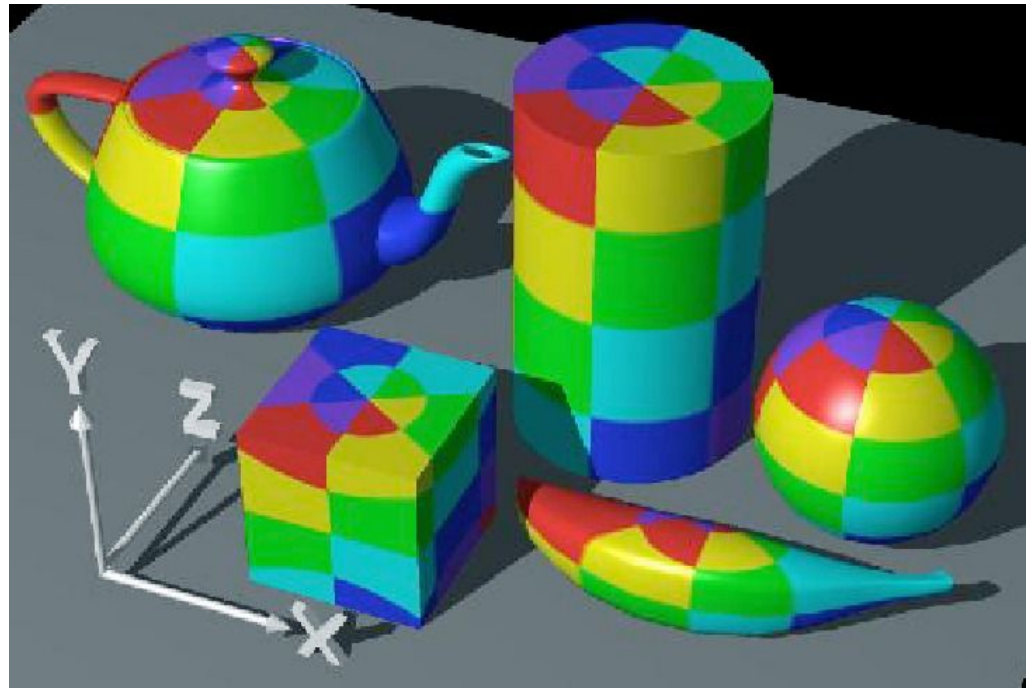
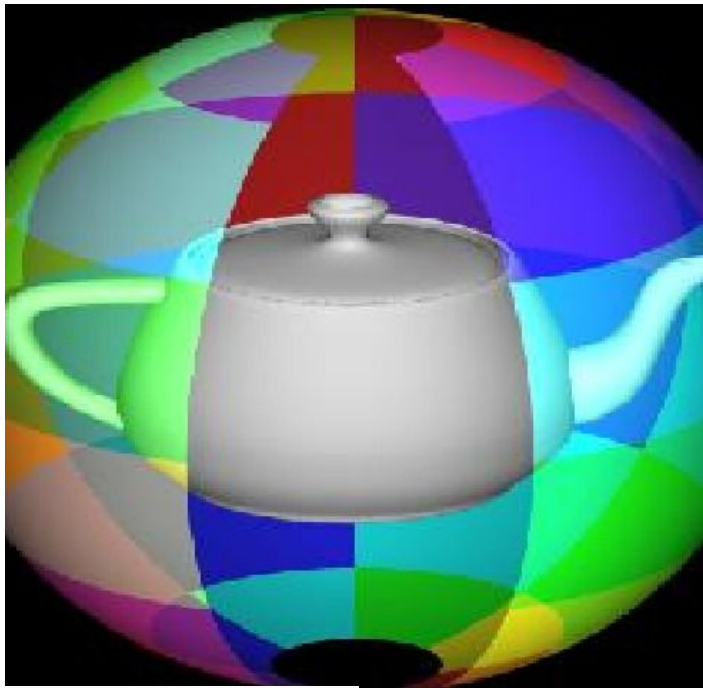


Synthetic rendering

Mapping function: spherical mapping

$f: (x,y,z) \rightarrow [0,1] \times [0,1]$

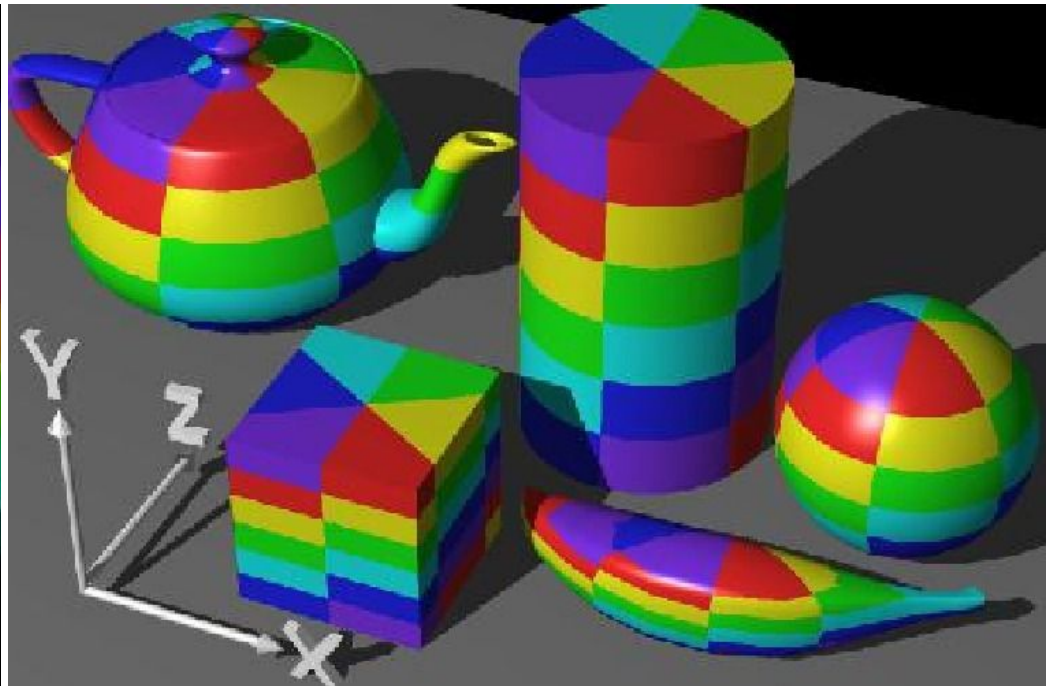
- Spherical mapping: $\mathbf{f}(\theta, \psi) = (\theta/2\pi, (\pi/2 - \psi) / \pi/4)$



Mapping function: cylindrical mapping

$f: (x,y,z) \rightarrow [0,1] \times [0,1]$

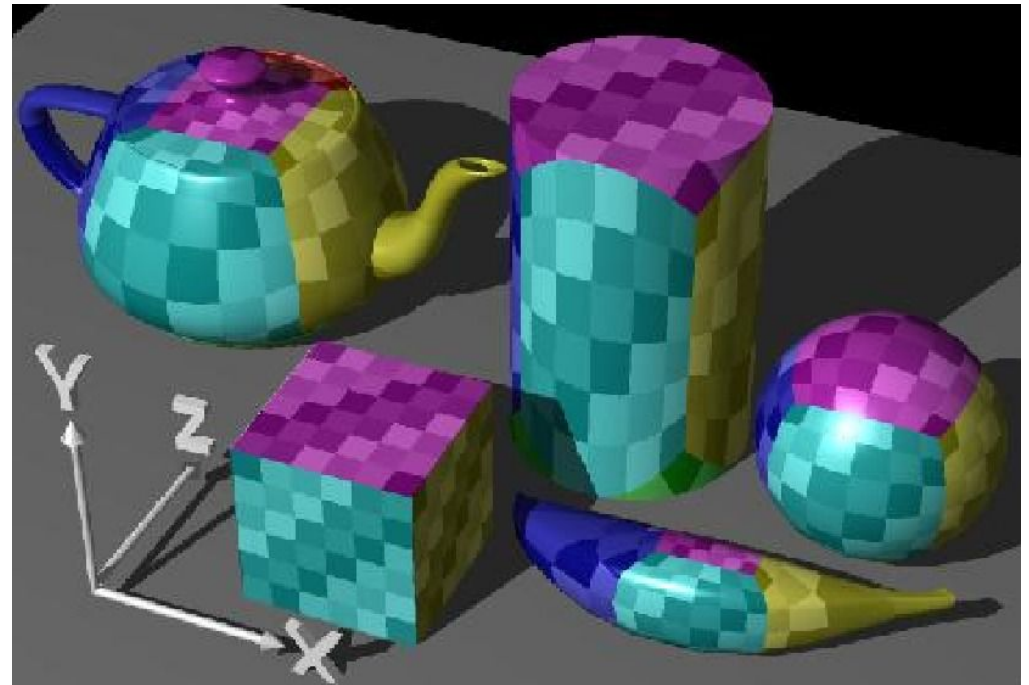
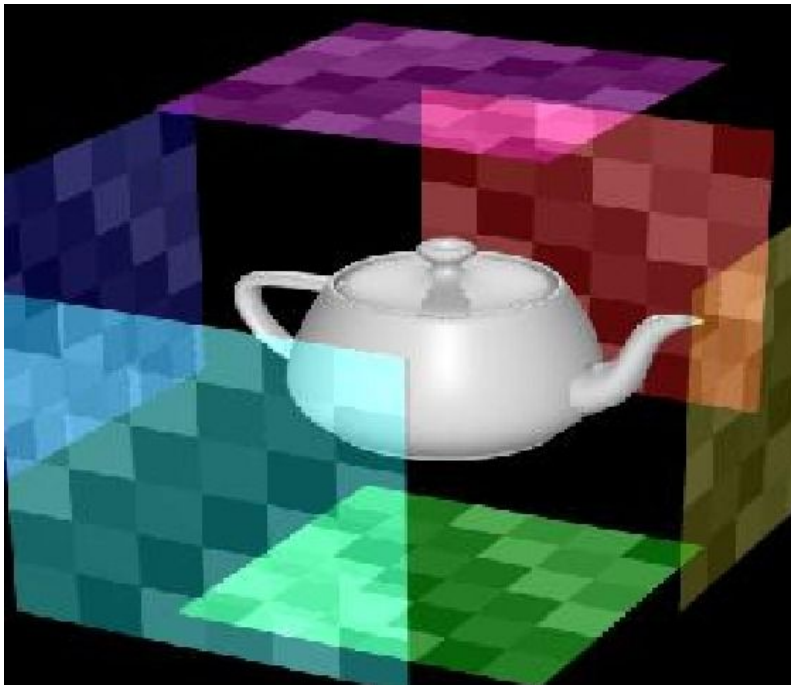
- Cylindrical mapping: $\mathbf{f}(\theta, z) = (\theta/2\pi, z)$



Mapping function: cube mapping

$$f: (x,y,z) \rightarrow [0,1] \times [0,1]$$

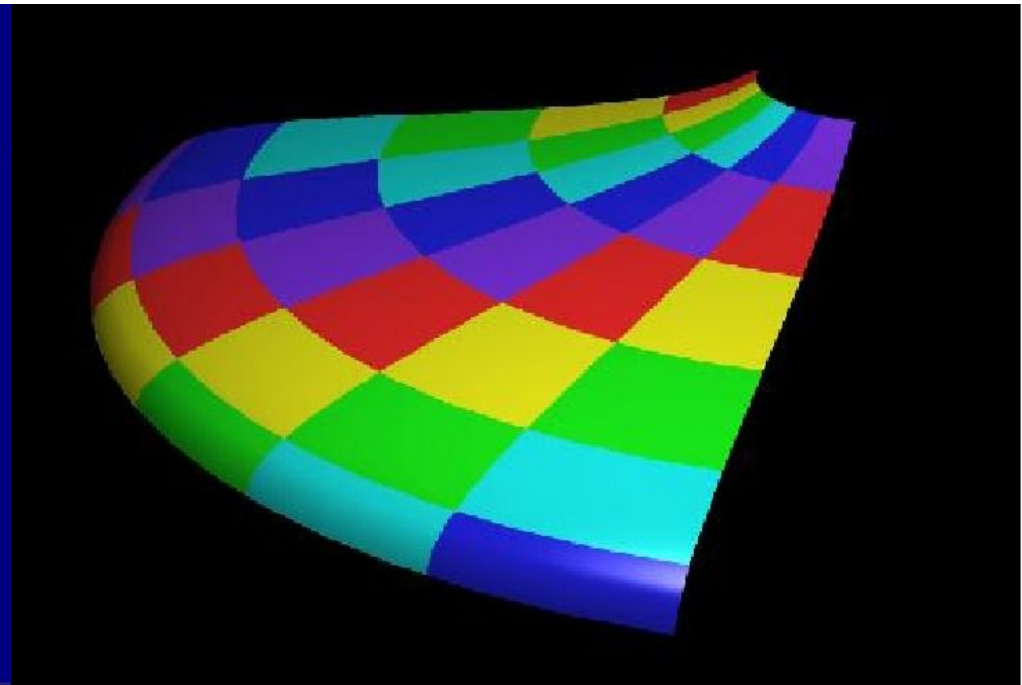
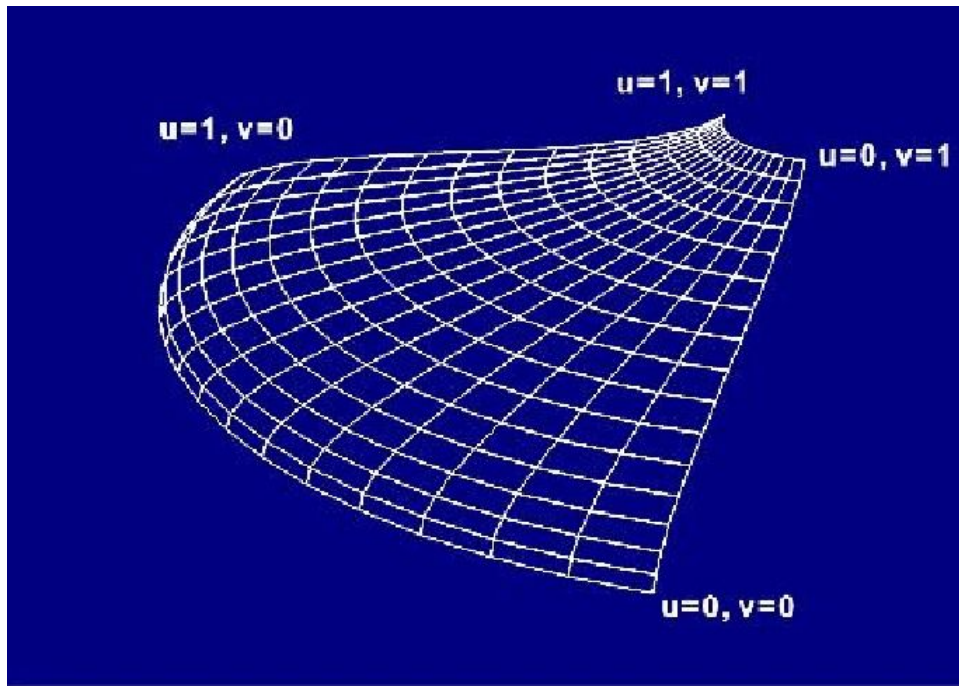
- Cube mapping: **depends on x,y,z signs**



Mapping function: parametric mapping

$$f: (x,y,z) \rightarrow [0,1] \times [0,1]$$

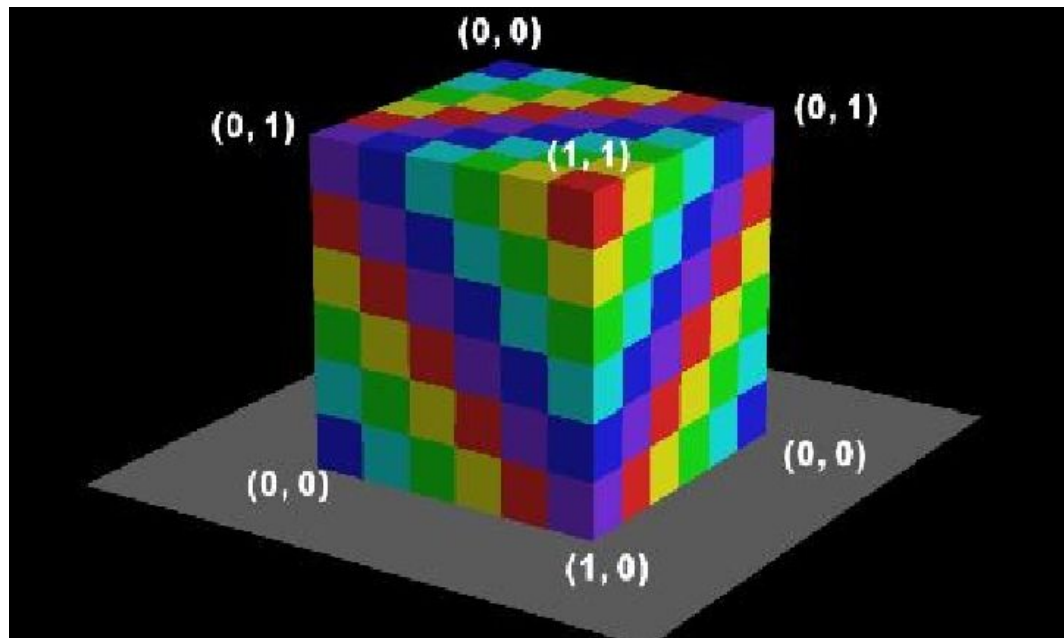
- Parametric mapping: $f(S(u,v)) = (u,v)$



Mapping function: uv mapping

$f: (x,y,z) \rightarrow [0,1] \times [0,1]$

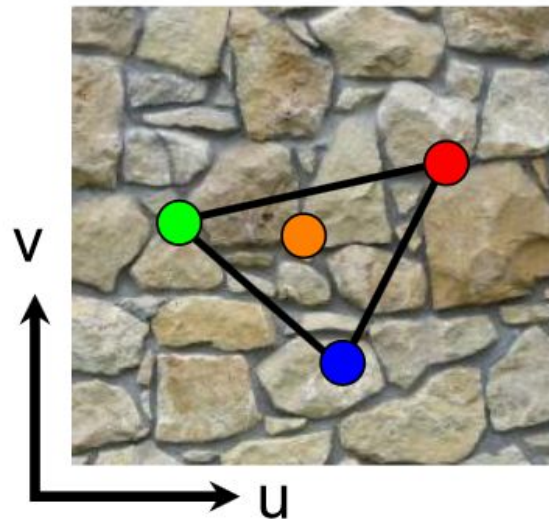
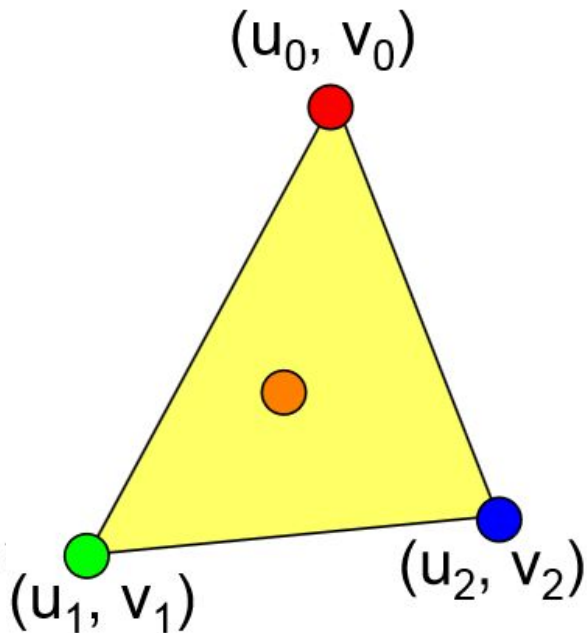
- UV mapping: define uv at each vertex and exploit rasterization



Rosalee Wolfe / siggraph.org

2D Textures: picture of attributes + mapping

- Planar image $I(u,v)$ + mapping $f: P(x,y,z) \rightarrow (u,v)$
- Store: mesh point + normal + texture coordinates (u,v)
- In a face, interpolate (u,v) using barycentric coords



Aliasing problems

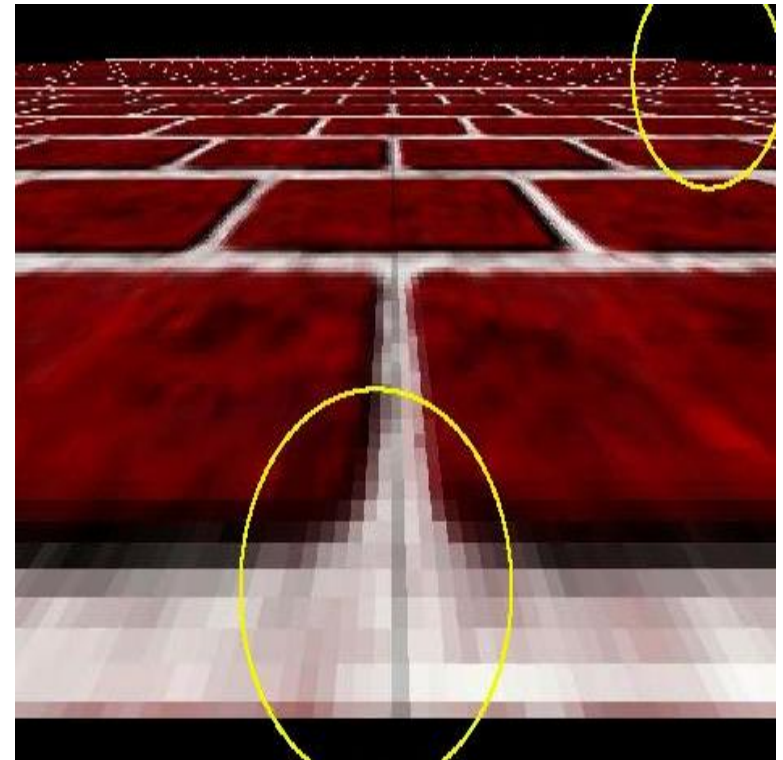
Brick wall picture mapped on one face

At the front

- The texture pixels can be seen

At the back

- Many colors in the same pixel
- The one at the center is picked!



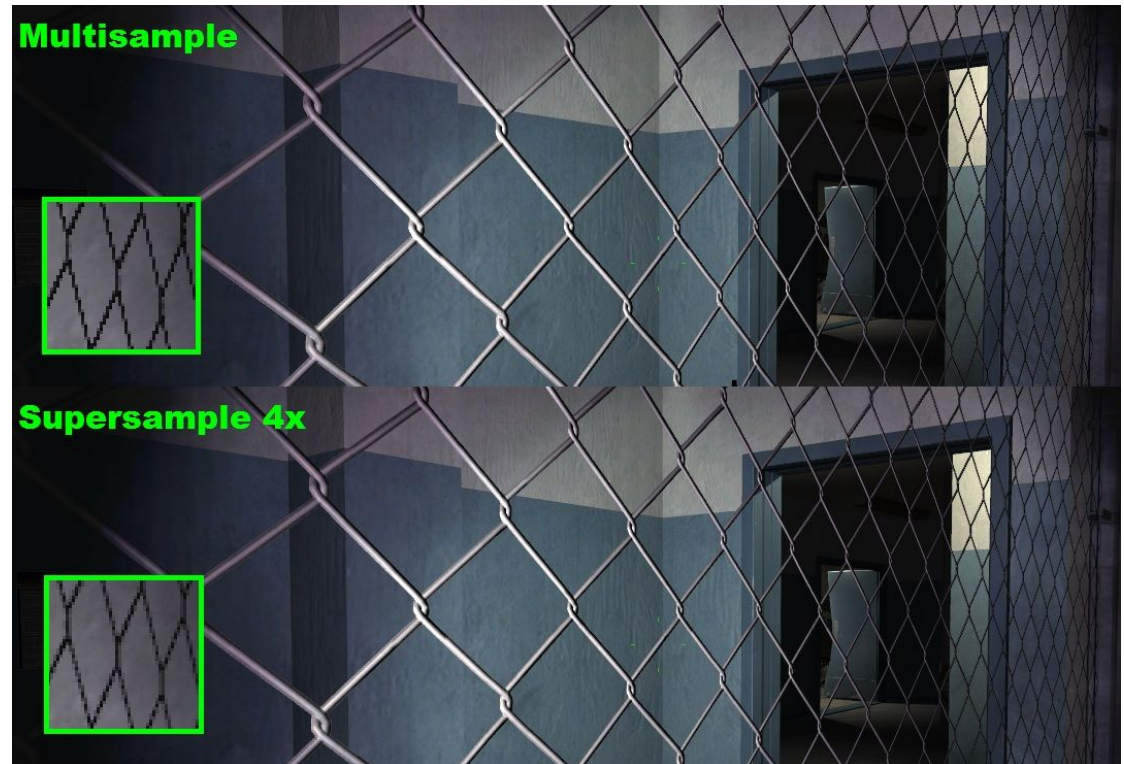
Aliasing problems

Solution 1: Pre-filtering

- compute multiple samples per pixel
- and average result

Advantage: “ground truth”

Drawback: expensive!



Aliasing problems

Solution 2: Pre-filtering

- Pre-compute an “image pyramid” (mip-map) of the texture: down sampling
- Pick the best texture resolution while rendering (rasterization phase)

Advantage: fast

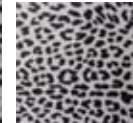
Drawback: incorrect filter



256x256



128x128



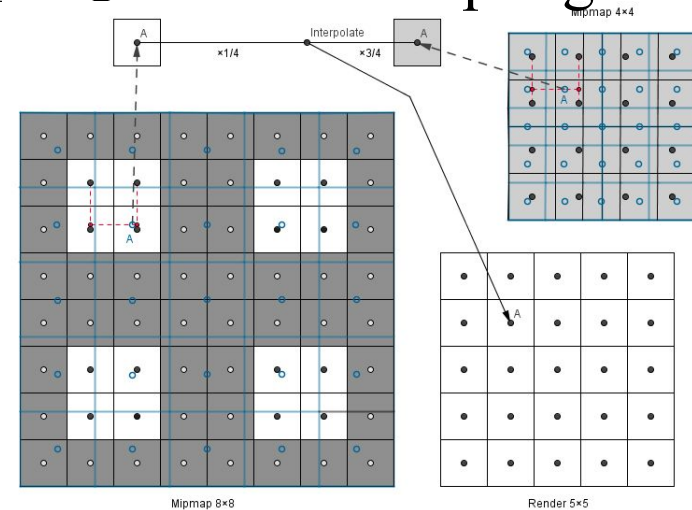
64x64



32x32

mip-map sampling

- Multiple options
 - Nearest scale, nearest neighbor texel sampling
 - Nearest scale, bilinear texel sampling
 - Trilinear sampling
- Trilinear sampling
 - Find nearest two scales
 - Bilinear sampling in each scale
 - Linear interpolation of the result

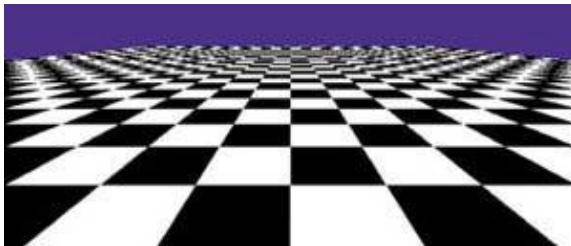


<https://cglearn.codelight.eu/pub/textures-and-sampling>

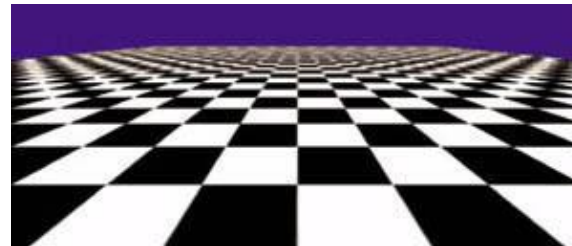
Mip-mapping

- Andrew Flavell has a nice (old) article on mip-mapping

http://www.gamasutra.com/view/feature/131708/runtime_mipmap_filtering.php



Without mip-mapping



With mip-mapping

Aliasing problems

Solution 3: Post-filtering

- screen-space anti-aliasing (SSAA)
- multiple algorithms
- more and more used

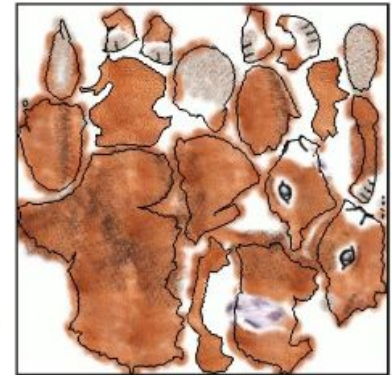
Advantage: fast, GPU friendly

Drawback: cannot handle all
types of artifacts

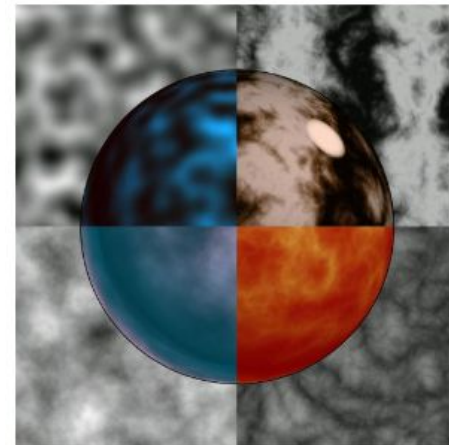


Creating a texture

- From real data
 - colors/normals/coefs,
 - stored in 2D images

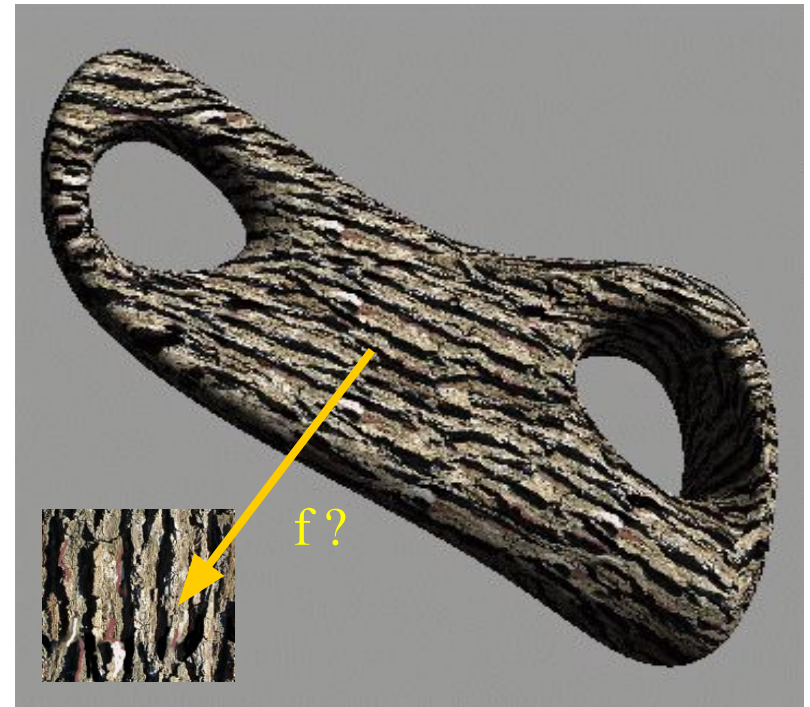
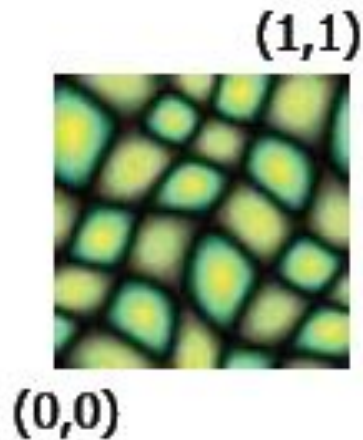


- Procedurally
 - using a small program
 - usually on the GPU



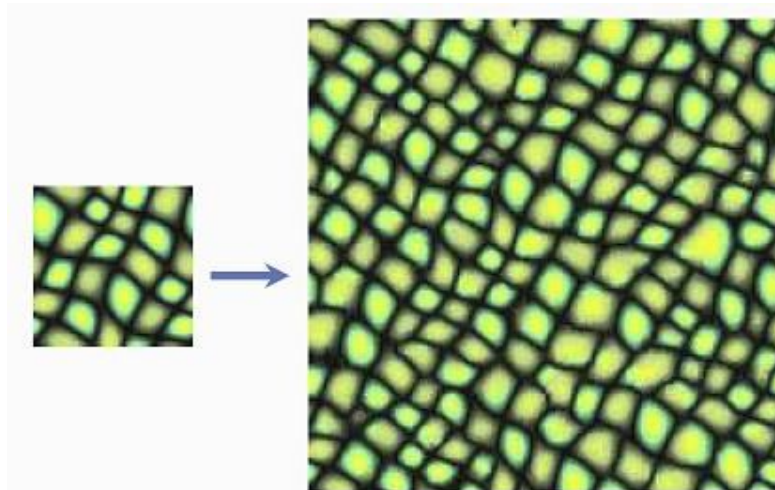
Creating a texture

- From real data
 - Paint a self similar texture
 - use torus topology for textures



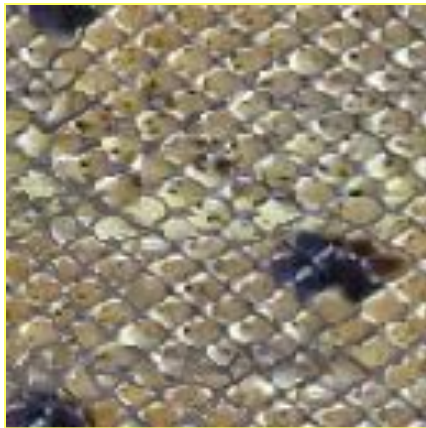
Creating a texture

- From real data
 - texture synthesis
 - analyse a small sample
 - generate a large similar texture



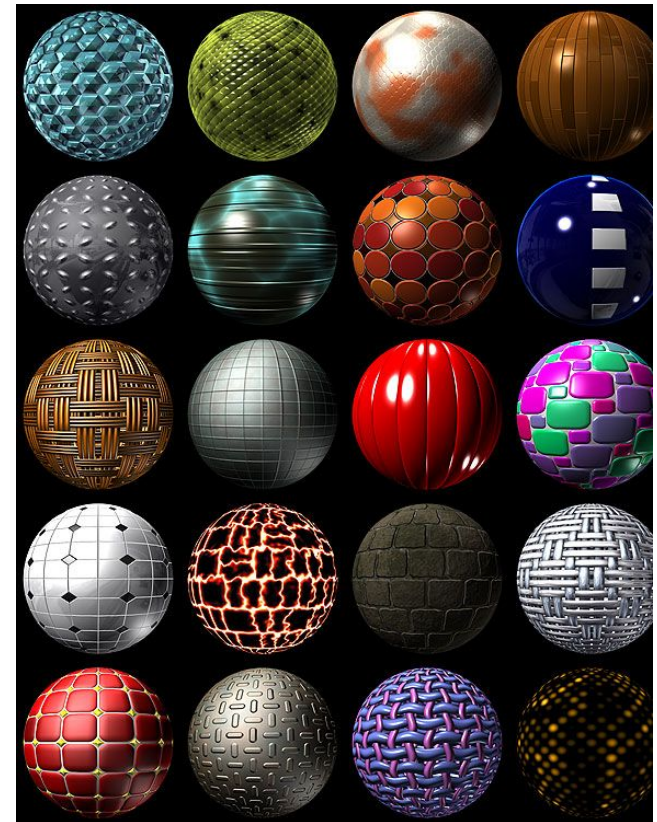
Creating a texture

- From real data
 - re-shading problem



Creating a texture

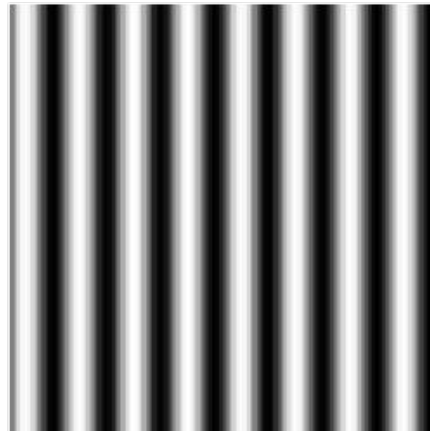
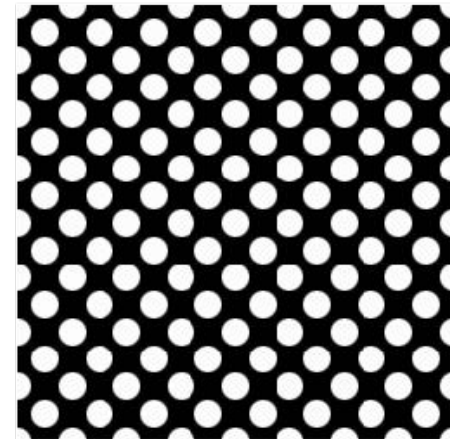
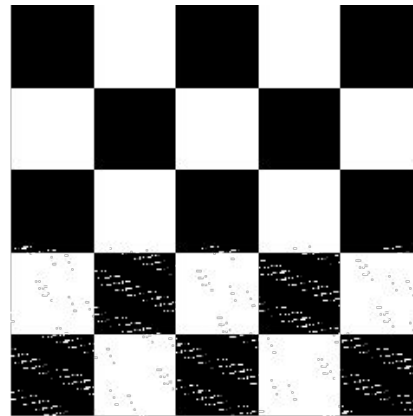
- Procedural
 - combination of simple functions
- + Easy to implement
- + Compact
- + Infinite resolution
- Non-intuitive
- Difficult to match existing textures



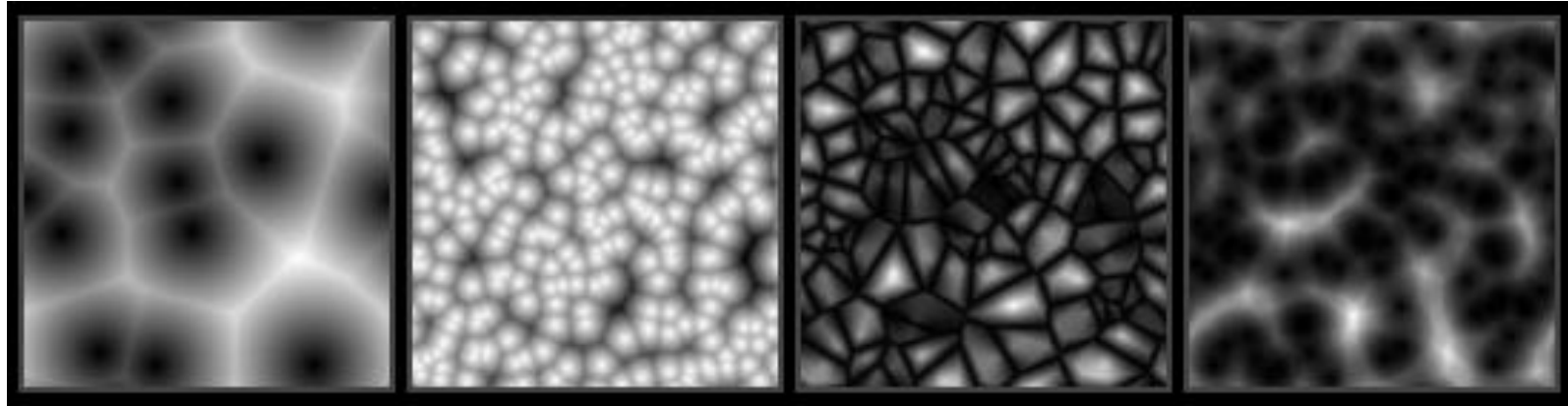
Procedural textures

- Combination of simple functions

- Mod
- Clamp
- Mix
- Sin / cos / tan
- Pow
- Exp
- Etc...



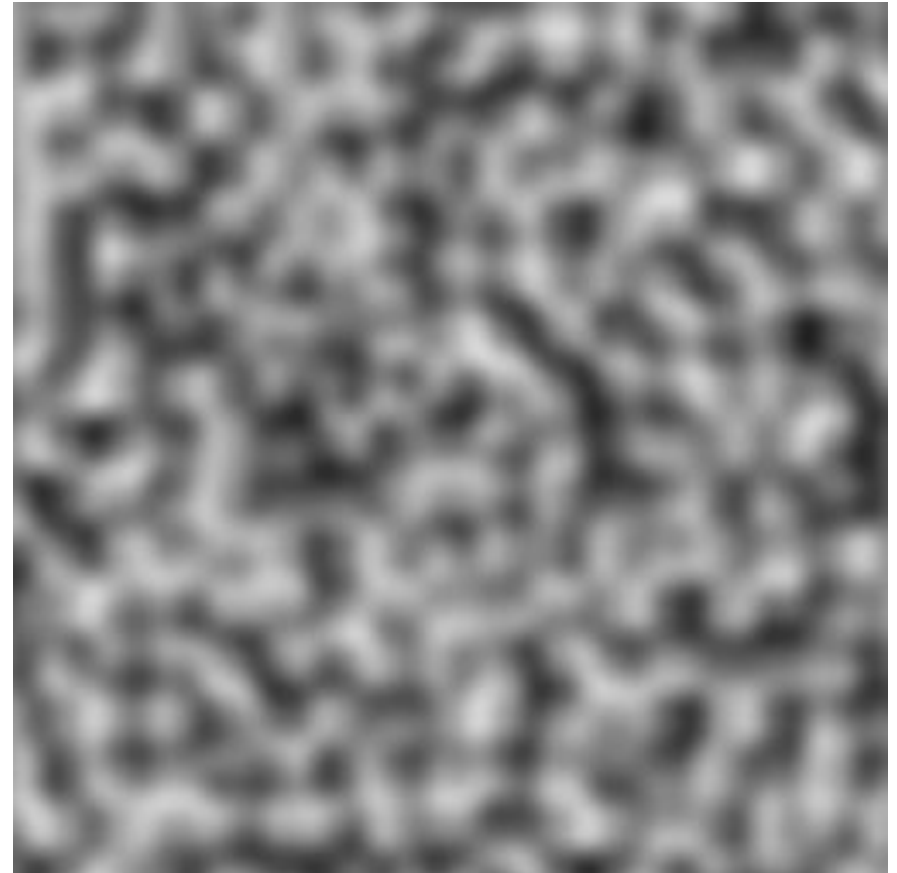
Procedural cellular textures



- Generate a bunch of random points
- For each pixel
 - Find the nearest distance to the nearest couple points
 - Use these values to determine a color
- Voronoi-like

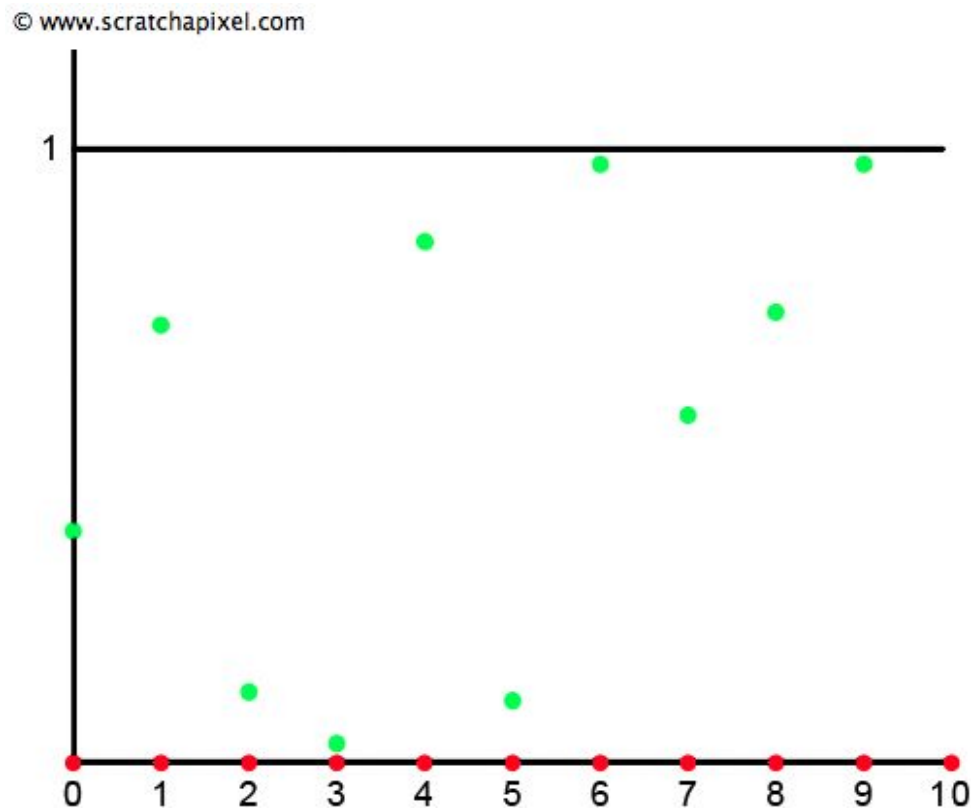
Perlin textures

- Requirements
 - Pseudo random
 - Arbitrary dimension
 - Smooth
 - Band pass (one scale)
 - Little memory usage
 - Implicit evaluation



Perlin textures

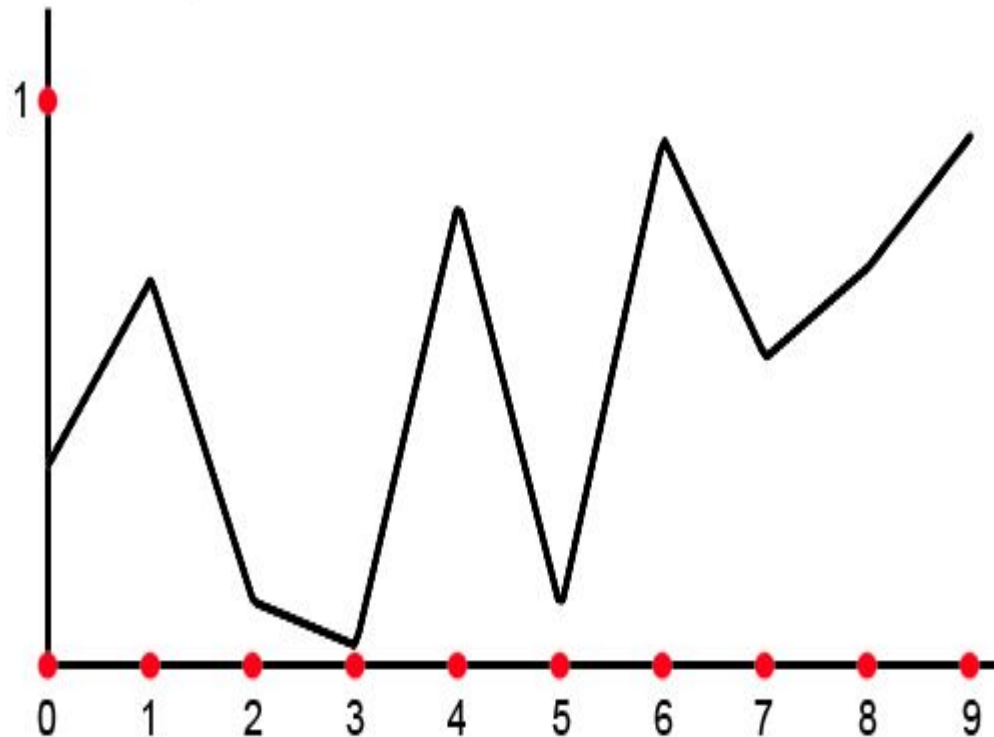
- Distribute random values at particular locations (a grid)...



Perlin textures

- Distribute random values at particular locations (a grid)...
- ... and interpolate

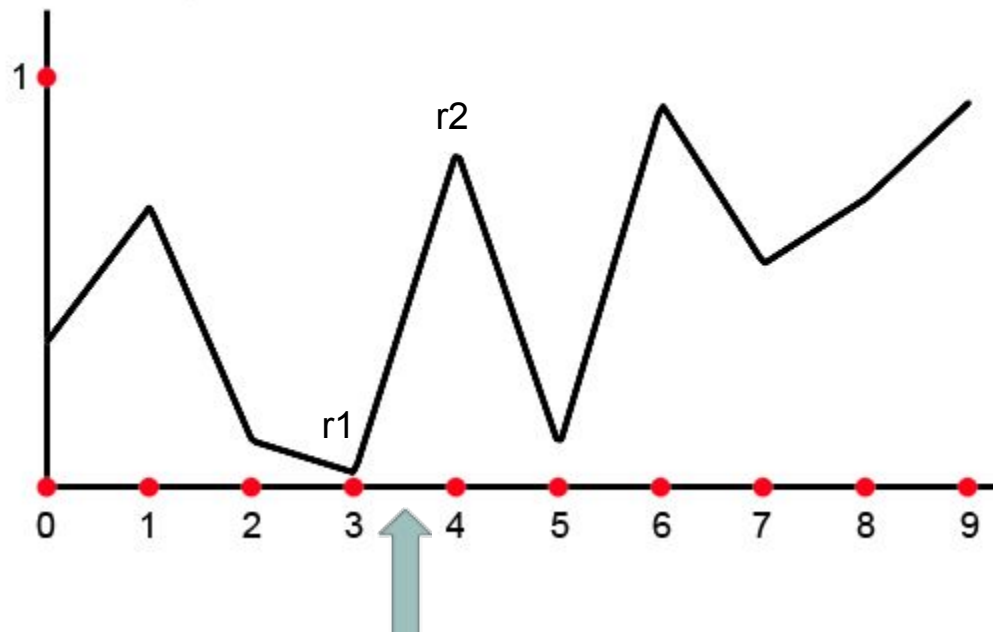
© www.scratchapixel.com



Perlin textures

- At a given point:

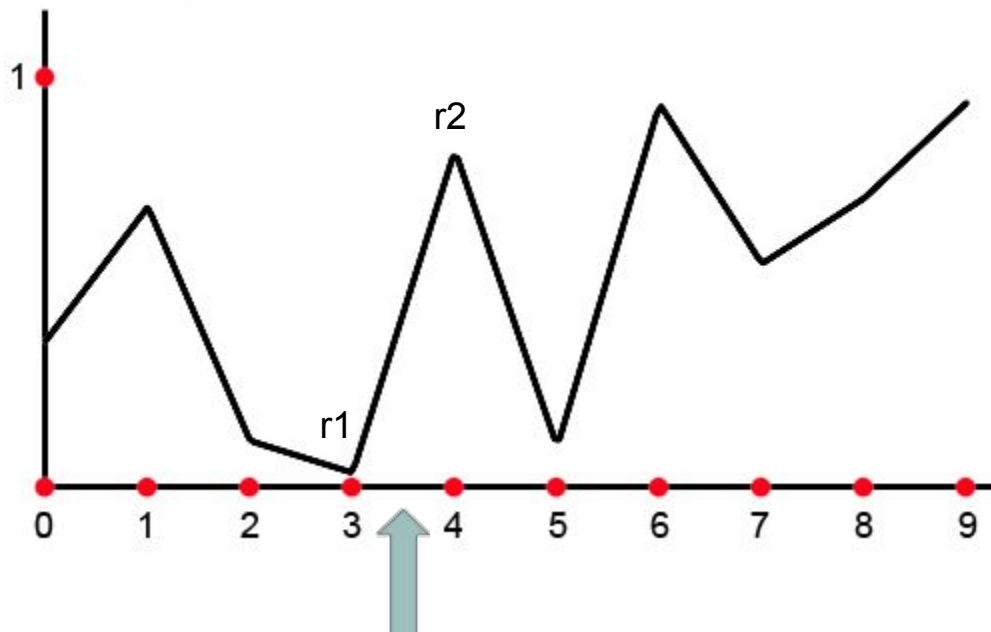
© www.scratchapixel.com



Perlin textures

- At a given point:
 - Get the associated 2 random values?

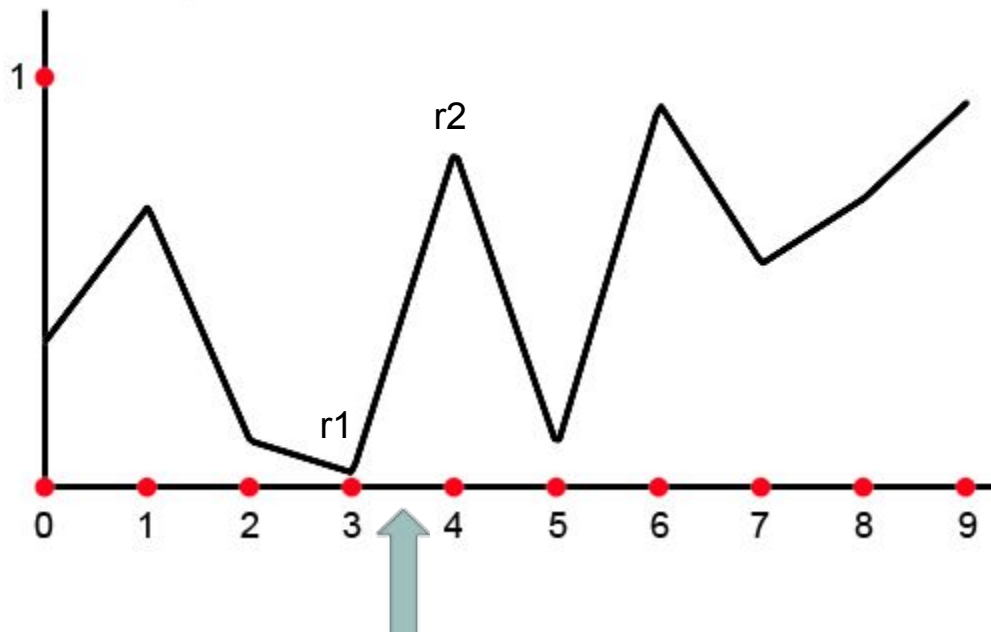
© www.scratchapixel.com



Perlin textures

- At a given point:
 - Get the associated 2 random values?
 - Pseudo random function
 - Precomputed in an array

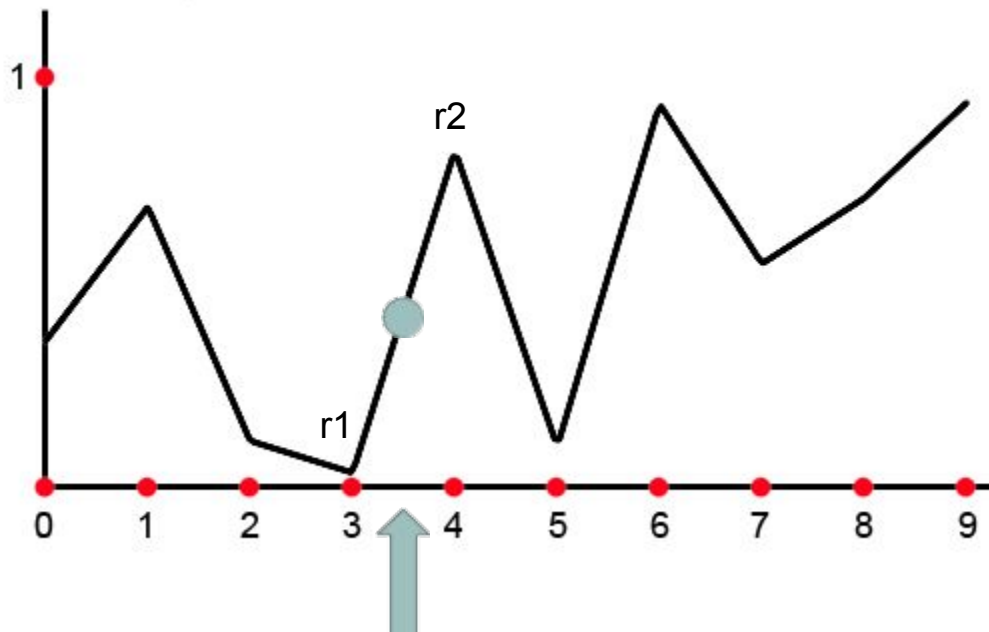
© www.scratchapixel.com



Perlin textures

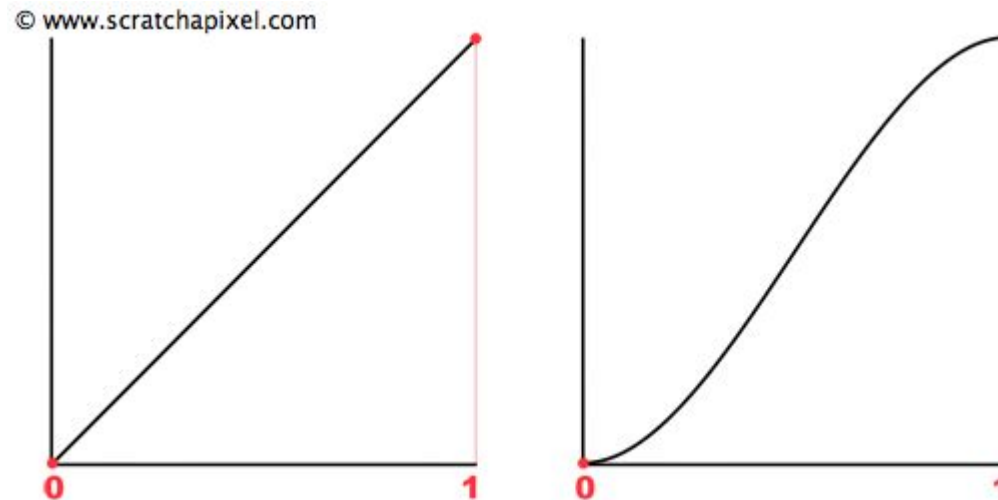
- At a given point:
 - Get the associated 2 random values?
 - Pseudo random function
 - Precomputed in an array
 - Get relative position of x (between 0 and 1)
 - mix!

© www.scratchapixel.com



Perlin textures

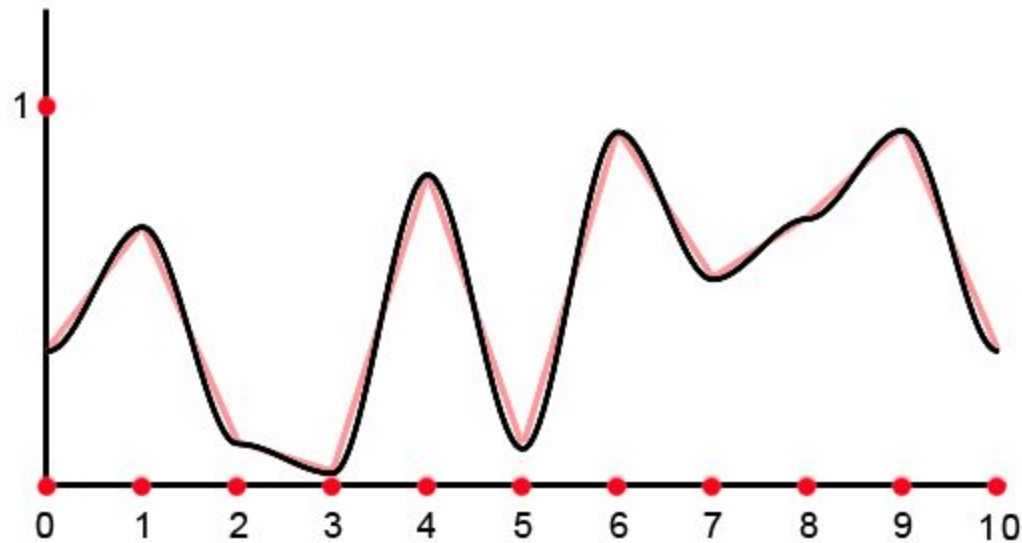
- At a given point:
 - Get the associated 2 random values?
 - Pseudo random function
 - Precomputed in an array
 - Get relative position of x (between 0 and 1)
 - mix!



S-Shaped function: $t = t^2(3 - 2t)$

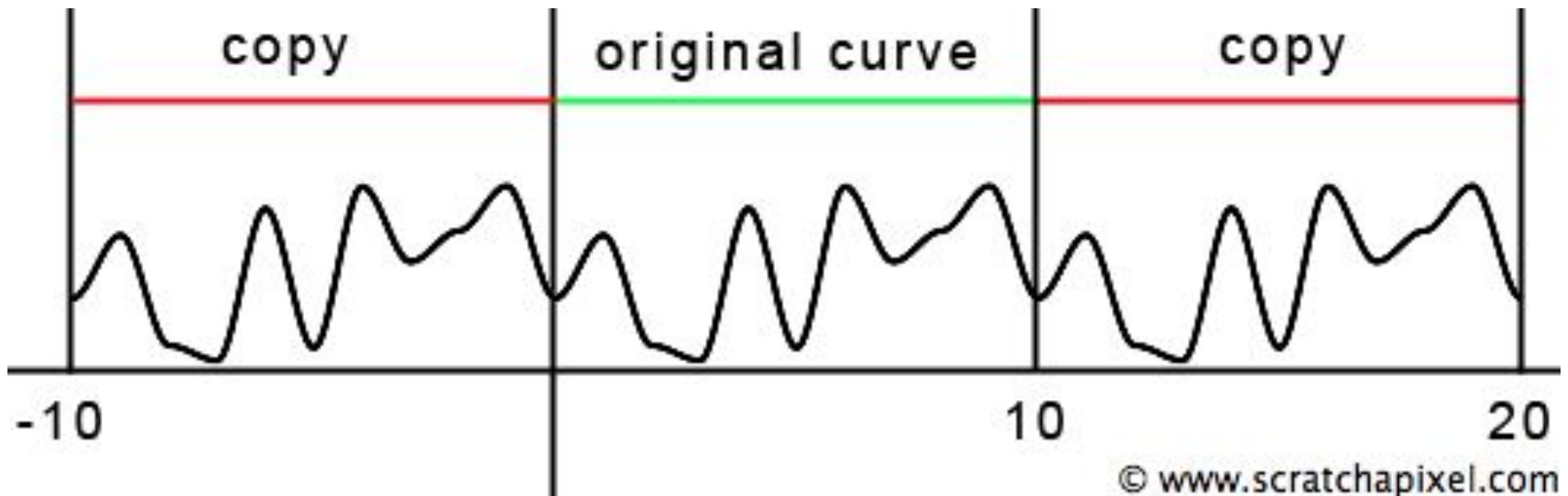
Perlin textures

- At a given point:
 - Get the associated 2 random values?
 - Pseudo random function
 - Precomputed in an array
 - Get relative position of x (between 0 and 1)
 - mix!



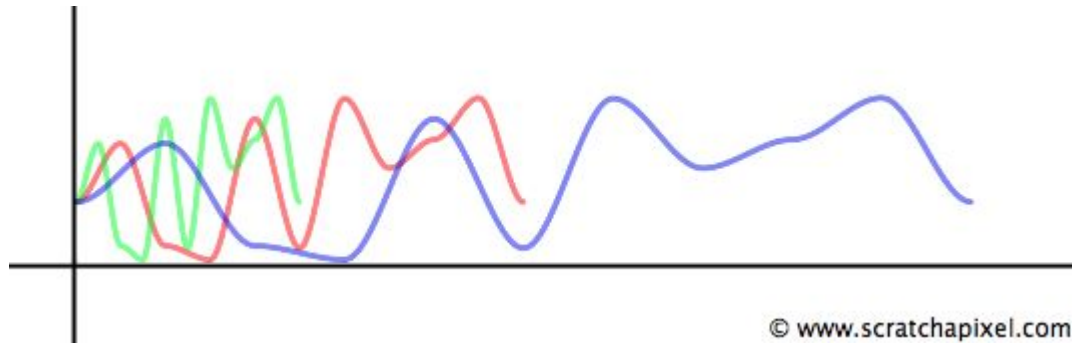
Perlin textures

- At a given point:
 - Get the associated 2 random values?
 - Pseudo random function
 - Precomputed in an array
 - Get relative position of x (between 0 and 1)
 - mix!



Perlin textures

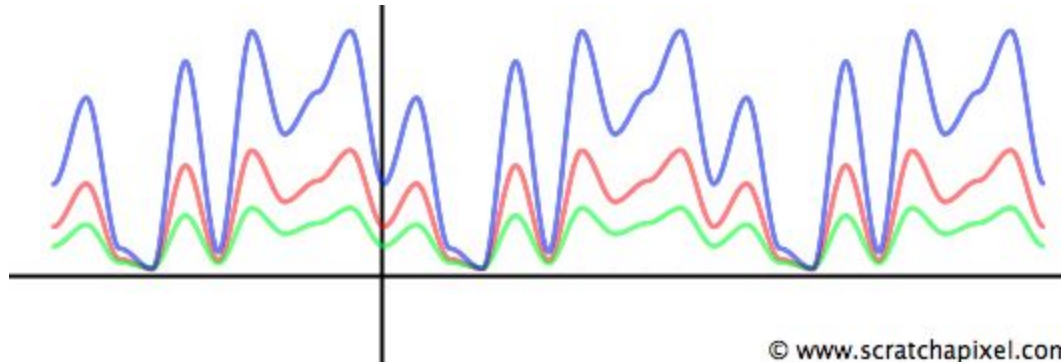
- Controls
 - Frequency: `evalNoise(x * freq)`



Perlin textures

- Controls

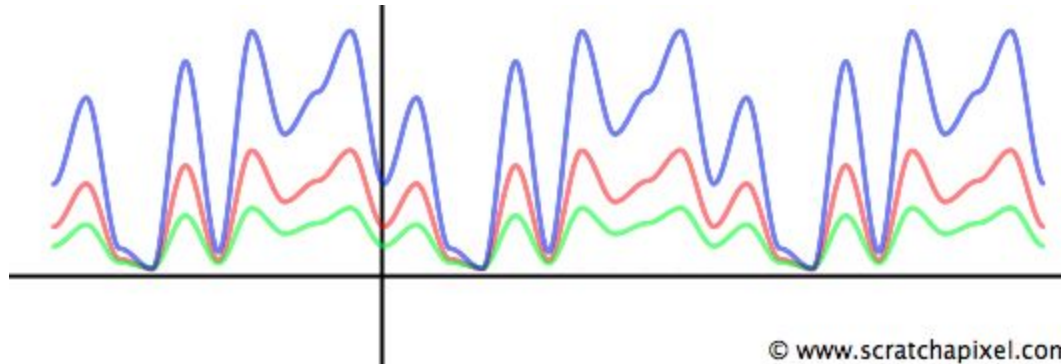
- Frequency: `evalNoise(x * freq)`
- Amplitude: `evalNoise(x) * amplitude`



Perlin textures

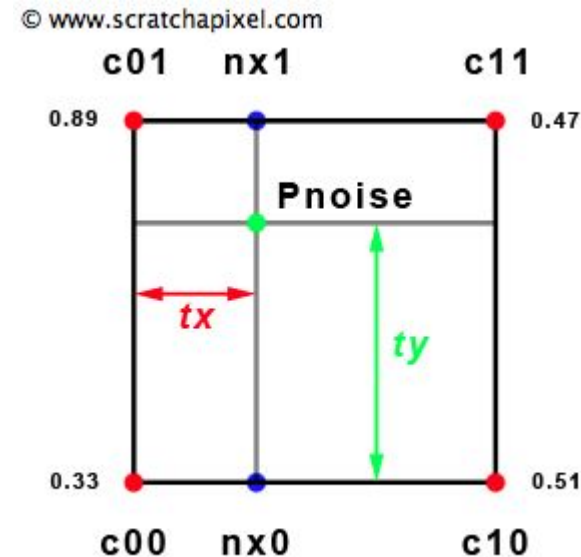
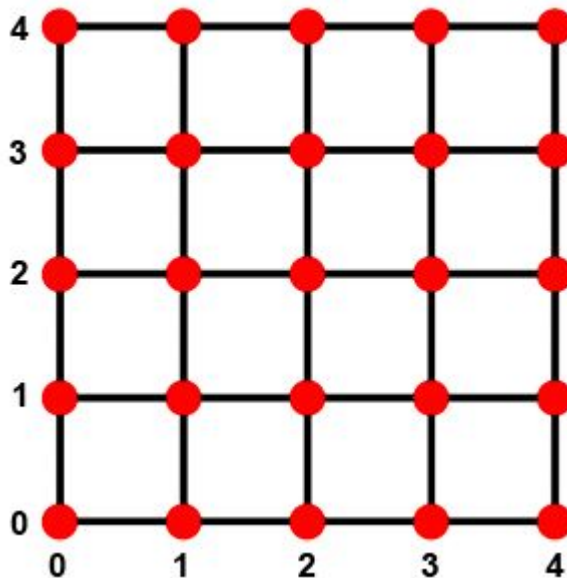
- Controls

- Frequency: `evalNoise(x * freq)`
- Amplitude: `evalNoise(x) * amplitude`
- Offsetting: `evalNoise(x + offset)`



Perlin textures

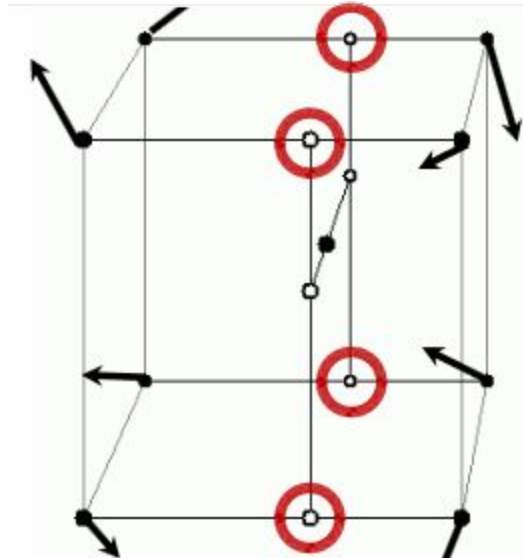
- In 2D
 - needs a 2D grid
 - requires 3 interpolations instead of 1



demo: <https://www.shadertoy.com/view/lsf3WH>

Perlin textures

- In 3D
 - same principle, with a 3D grid
 - requires 7 interpolations

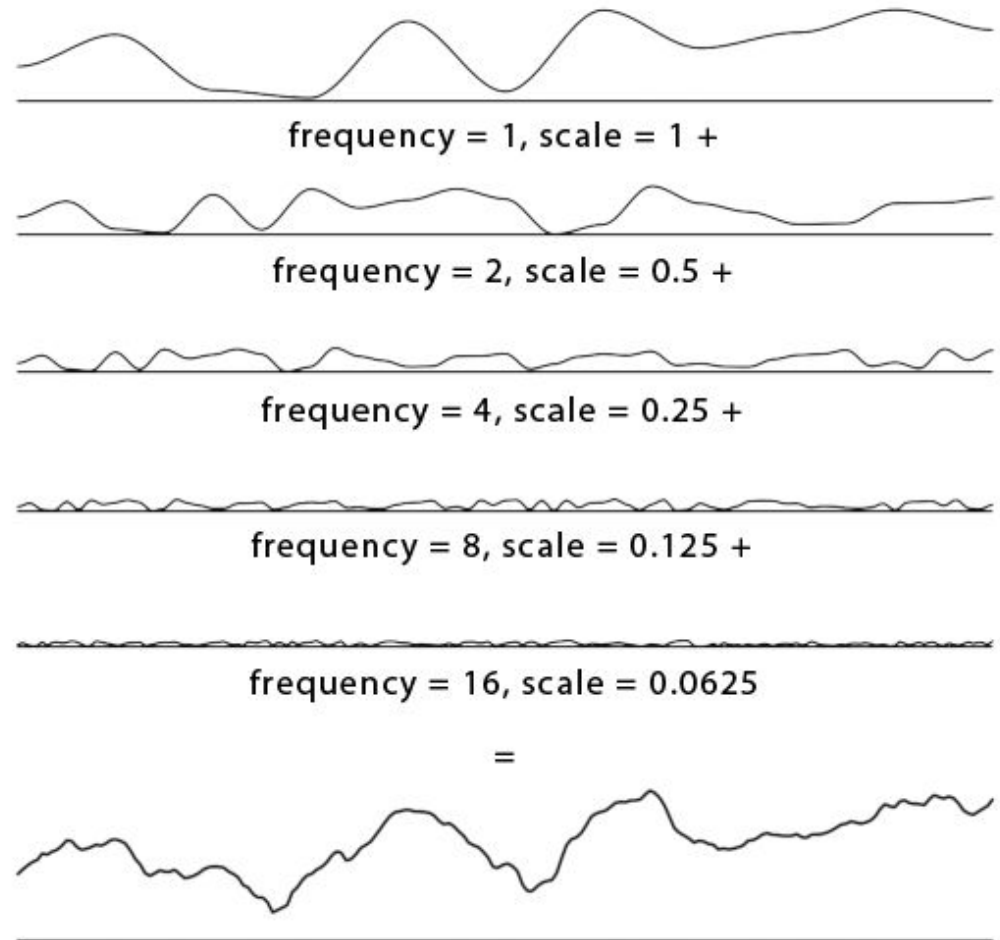


demo: <https://www.shadertoy.com/view/XsXfRH>

Fractal Perlin textures

© www.scratchapixel.com

- Noise at one scale = 1 octave
- Multiple octave usually used
 - Frequency multiplied by 2 each time
 - Hence the name octave
 - Different amplitudes too
- Sum of all noises =
 - Fractal noise

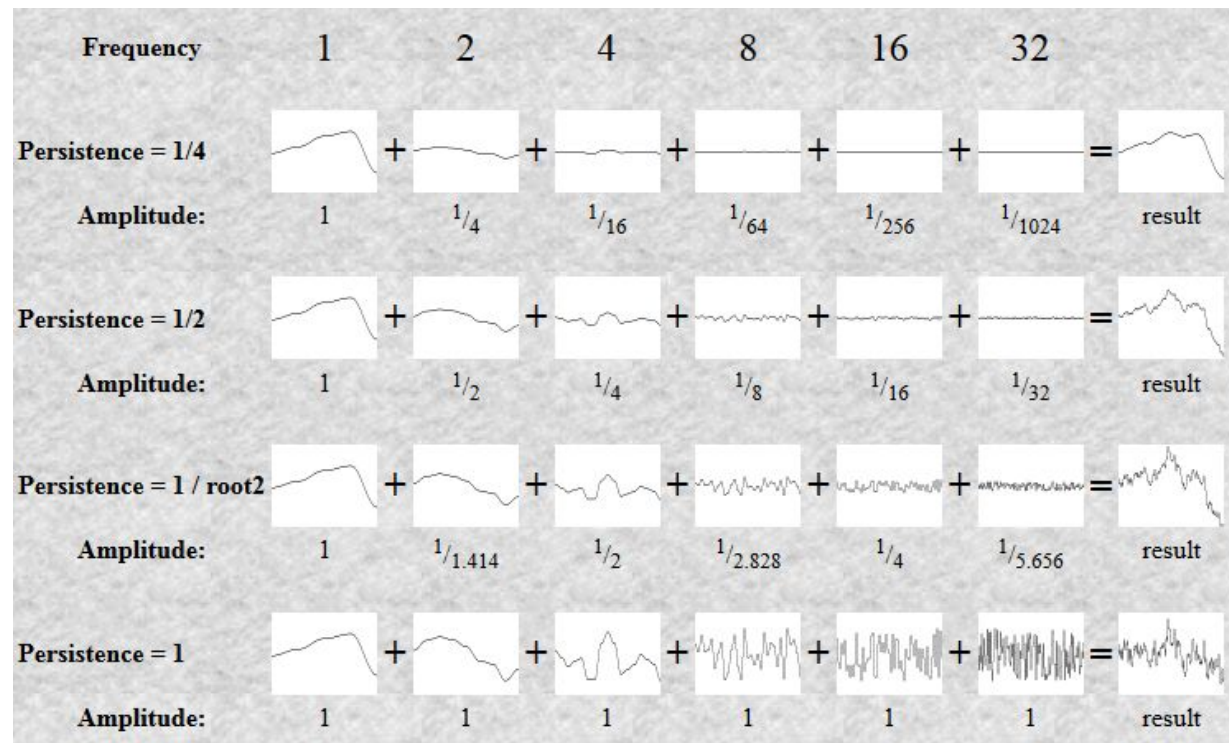


Fractal Perlin textures

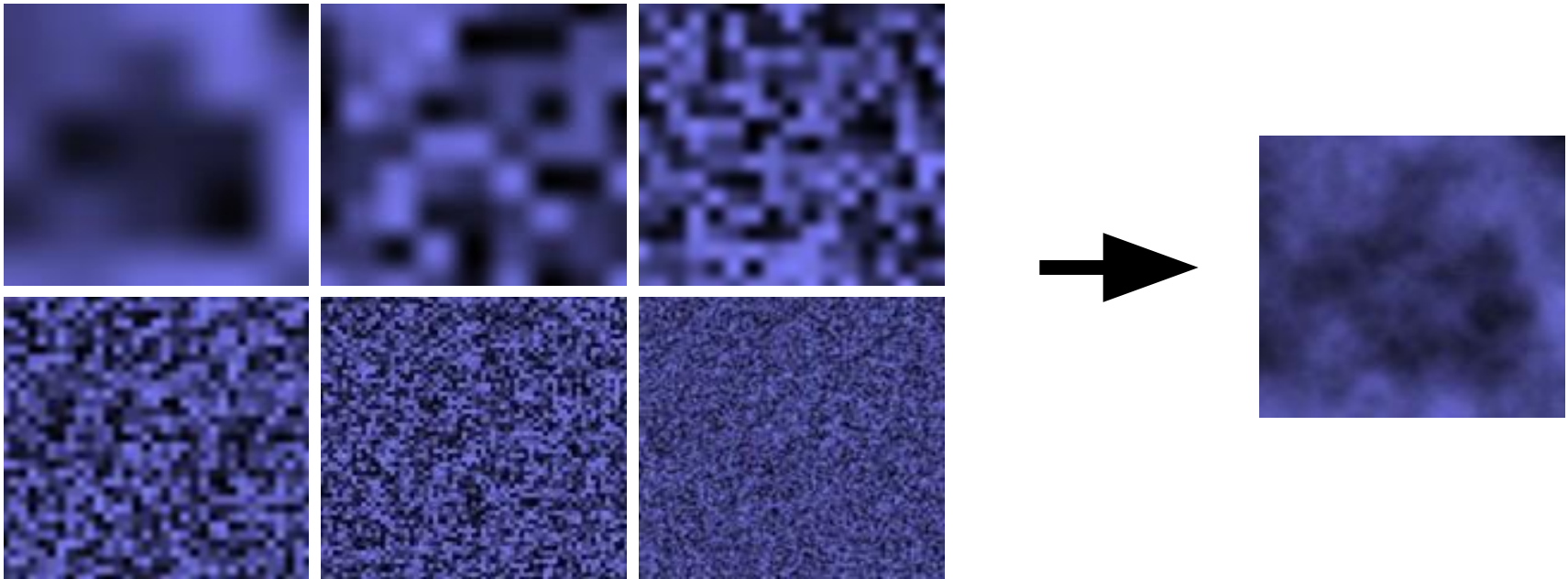
- Compute the i th texture using:

$$\text{frequency} = 2^i$$

$$\text{amplitude} = \text{persistence}^i \quad (\text{relation between frequency and amplitude})$$



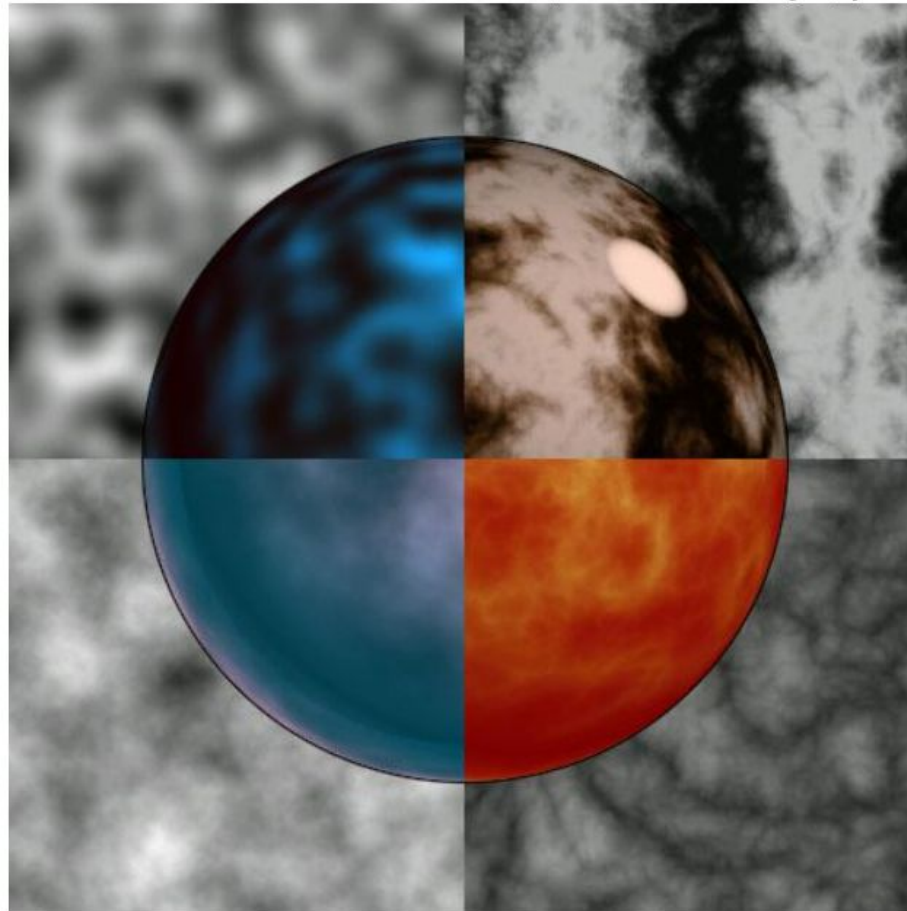
Fractal Perlin textures



Fractal Perlin textures

•noise

$\sin(x + \sum 1/f(|noise|))$



$\sum 1/f(noise)$

$\sum 1/f(|noise|)$

Fractal Perlin textures

- Marble

$$\begin{aligned} & \text{Sin} (x + \text{Sum } 1/f(\text{noise})) \\ & = \\ & \text{Colormap}(\text{Sin} (x + \text{turbulence})) \end{aligned}$$



- Wood

$$\text{Colormap}(\text{Sin} (\text{radius} + \text{turbulence}))$$



Perlin's textures : Examples

